

Test of the flavour independence of α_s using next-to-leading order calculations for heavy quarks

The OPAL Collaboration

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Abstract. We present a test of the flavour independence of the strong coupling constant for charm and bottom quarks with respect to light (uds) quarks, based on a hadronic event sample obtained with the OPAL detector at LEP. Five observables related to global event shapes were used to measure α_s in three flavour tagged samples (uds, c and b). The event shape distributions were fitted by $\mathcal{O}(\alpha_s^2)$ calculations of jet production taking into account mass effects for the c and b quarks. We find:

$$\begin{aligned} \alpha_s^c / \alpha_s^{\text{uds}} &= 0.997 \pm 0.038 \text{ (stat.)} \pm 0.030 \text{ (syst.)} \pm 0.012 \text{ (theory)} \quad \text{and} \\ \alpha_s^b / \alpha_s^{\text{uds}} &= 0.993 \pm 0.008 \text{ (stat.)} \pm 0.006 \text{ (syst.)} \pm 0.011 \text{ (theory)}. \end{aligned}$$

1 Introduction

According to the theory of strong interactions, Quantum Chromodynamics (QCD) [1], the strong coupling constant α_s is the same for all quark flavours. Therefore a precise measurement of α_s for the individual quark flavours is an important test of this theory. The coupling constant α_s for charm and bottom quarks can be compared to α_s for light (uds) quarks by measuring the ratios $\alpha_s^c/\alpha_s^{\text{uds}}$ and $\alpha_s^b/\alpha_s^{\text{uds}}$ using hadronic events of the type $e^+e^- \rightarrow q\bar{q}g$. The coupling constants are measured using an event sample originating from a pair of light quarks ($u\bar{u}$, $s\bar{s}$ or

$d\bar{d}$), c quarks ($c\bar{c}$) or b quarks ($b\bar{b}$), respectively. If either of the above ratios deviates significantly from unity then this may indicate physics beyond the Standard Model.

In high-energy QCD studies corrections due to quark mass effects can be safely ignored because they typically appear as powers of the ratio of the quark mass to the total energy. However, in those studies where α_s is determined in event samples enriched in heavy quarks, mass effects become non-negligible. Gluon emission by bottom quarks, and to a lesser extent charm quarks, will be suppressed largely due to the reduced phase-space available. Observables sensitive to the three-jet rate measured in heavy quark events will be modified with respect to the same quantities measured in light quark events.

Tests of the flavour independence of α_s have previously been conducted at both LEP and SLC [2–7] using ratios of α_s for one flavour over α_s of either the complementary¹ or inclusive quark mixture. In all these tests flavour independence of α_s was confirmed. These tests, however,

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¹ For example, α_s for c quarks was compared to α_s for a mixture of u, d, s and b quarks

used either massless QCD calculations or a leading order calculation with massive quarks [8]. The leading order calculation includes the process $e^+e^- \rightarrow q\bar{q}gg$, with mass effects, but virtual corrections to the process $e^+e^- \rightarrow q\bar{q}g$ are not included.

Complete next-to-leading-order (NLO) calculations of the heavy-flavour production cross section in e^+e^- collisions, including quark mass effects, have been published recently [9–11]. A comparison between these calculations has been made and they were found to be in agreement [11]. In recent publications DELPHI [12] and SLD [13] report on measurements of $\alpha_s^b/\alpha_s^{\text{uds}}$ where NLO massive calculations [9,10] were used to account for mass effects in b quark events. These results are consistent with the flavour independence of α_s .

In this study we use the results of P. Nason and C. Oleari [11] along with theoretical predictions assuming massless quarks in fits to global event shape distributions in order to determine α_s^{uds} , $\alpha_s^c/\alpha_s^{\text{uds}}$ and $\alpha_s^b/\alpha_s^{\text{uds}}$. The results presented here are intended to update and supersede the corresponding OPAL results in [2,3] insofar as we now have greatly increased the charm event statistics and have used improved theoretical predictions.

This paper is organised as follows. In Sect. 2 the parts of the OPAL detector most important to this analysis are described. In Sect. 3 the hadronic event sample and the Monte Carlo event sample are introduced. In Sect. 4 and 5 the flavour tagging methods are described. In Sect. 6 the event shape observables used in this study are introduced and the procedure for correcting the event shape distributions is explained. Next, in Sect. 7, the procedure for fitting the NLO QCD prediction to the corrected distributions is explained and in Sect. 8 the systematic uncertainties that have been taken into account are discussed. In Sect. 9, the results of the test of flavour independence of α_s are presented. Finally, in Sect. 10, conclusions are drawn.

2 The OPAL detector

The OPAL detector operates at the LEP e^+e^- collider at CERN. A detailed description can be found in Refs. [14, 15]. The analysis presented here relies mainly on the reconstruction of charged particle trajectories and momenta in the central tracking chambers, on energy deposits (“clusters”) in the electromagnetic calorimeters and on information from the silicon micro-vertex detector.

All tracking systems are located inside a solenoidal magnet which provides a uniform magnetic field of 0.435 T along the beam axis². The magnet is surrounded by a lead glass electromagnetic calorimeter and a hadron calorimeter of the sampling type. Outside the hadron calorimeter,

² In the OPAL coordinate system the x axis points towards the centre of the LEP ring, the y axis points upwards and the z axis points in the direction of the electron beam. The polar angle θ and the azimuthal angle ϕ are defined with respect to the z - and x -axes, respectively, while r is the distance from the z -axis

the detector is surrounded by a system of muon chambers. There are similar layers of detectors in the barrel ($|\cos\theta| < 0.82$) and endcap ($|\cos\theta| > 0.81$) regions.

The central tracking detector consists of a silicon micro-vertex detector [15] and three drift chamber devices: the vertex detector, a large jet chamber, and surrounding z -chambers. The silicon micro-vertex detector, close to the beam pipe, consists of two layers of silicon strips with a single-hit resolution of about $7\mu\text{m}$ in the $r\phi$ plane. The vertex chamber is a cylindrical drift chamber covering a range of $|\cos\theta| < 0.95$. Its single hit resolution is $50\mu\text{m}$ in the $r\phi$ plane and $700\mu\text{m}$ in the z direction. The jet chamber is a cylindrical drift chamber with an inner radius of 25 cm, an outer radius of 185 cm, and a length of about 4 m. Its spatial resolution is about $135\mu\text{m}$ in the $r\phi$ plane from drift time information and about 6 cm in the z direction from charge division. The z -chambers provide a more accurate z measurement with a resolution of about $300\mu\text{m}$. In combination, the three drift chambers yield a momentum resolution of $\sigma_{p_t}/p_t \approx \sqrt{0.02^2 + (0.0015 \cdot p_t)^2}$ for $|\cos(\theta)| < 0.7$, where p_t is the transverse momentum in GeV/ c .

Electromagnetic energy is measured by lead glass calorimeters surrounding the solenoid magnet coil. They consist of a barrel and two endcap arrays with a total of 11704 lead glass blocks covering a range of $|\cos\theta| < 0.98$.

3 Event sample and Monte Carlo simulation

This analysis is based on a sample of 4.4 million hadronic decays of the Z^0 recorded with the OPAL detector between 1990 and 1995. Hadronic Z^0 decays were selected by placing requirements on the number of reconstructed tracks and the energy deposited in the calorimeter. A detailed description of the criteria is given in [16]. The parts of the detector essential for the present analysis (central detector and electromagnetic calorimeter) were required to be fully operational. The track selection criteria were the same as presented in a previous OPAL study [17]. The number of accepted tracks was required to be at least five to reduce $\tau^+\tau^-$ background. Clusters of electromagnetic energy were used if their observed energy was greater than 0.25 GeV, and known noisy channels in the detector were ignored. The event thrust axis [17] was determined using all accepted tracks and clusters, and its direction was required to fulfil the condition $|\cos\theta_{\text{Th}}| < 0.9$ in order that the event be well contained. Using these selection criteria, Monte Carlo studies indicate that, within the chosen range of $\cos\theta_{\text{Th}}$, 99.86 \pm 0.07% of hadronic Z^0 decays are accepted, with a contamination of about 0.14% from $\tau^+\tau^-$ events, and around 0.07% from two-photon interactions [17].

To correct the measured event shape distributions (see Sect. 6.1), 4 million hadronic decays of the Z^0 have been simulated using the JETSET 7.4 Monte Carlo model [18] with parameters tuned to reproduce OPAL data [19]. For all simulated events heavy quark fragmentation has been implemented using the model of Peterson et al. [20]. All events have been passed through a detailed simulation of

the OPAL detector [21] before being analysed using the same programs as for data.

4 Selection of uds and b quark events

Two event samples, one enriched in uds quark events and one enriched in b quark events, were selected by first determining the number of tracks in each event (N_{sig}) with a large impact parameter significance, $b/\sigma_b > 2.5$. Here b is the distance of closest approach in the xy plane of the track to the e^+e^- interaction point (IP) and σ_b its error. The sign of b was determined with respect to the crossing point between the track and the jet axis. b is positive if the track crosses the jet axis downstream of the IP and negative otherwise. An event was classified as having a high probability to have come from light quarks if N_{sig} was zero and from b quarks if $N_{sig} \geq 5$. In the text below these will be referred to as the “uds-tag” and the “b-tag” event samples.

For the uds and b quark event selection all data recorded during 1994 were used. This represents 1.4 million events. The analysis was restricted to only the 1994 data because of the uniform configuration of the silicon micro-vertex detector during this time period. In addition to the track selection criteria outlined above, the track was required to contain at least one silicon hit and an algorithm was applied to reject tracks which were consistent with arising from photon conversions [22]. In order for the event to be contained within the acceptance of the silicon micro-vertex detector the event’s thrust axis was further restricted to lie within the range $|\cos \theta_{Th}| < 0.7$.

The distribution of N_{sig} is shown in Fig. 1 compared with the result of Monte Carlo simulation. The simulation is decomposed into the contributions from uds, c and b quark events. The general agreement between the sum of the three contributions from Monte Carlo and the data is good.

This tagging procedure resulted in 325 111 events selected for the uds-tag event sample and 71 521 for the b-tag event sample. The flavour compositions of the uds-tag and the b-tag event samples as determined from the Monte Carlo, along with their combined statistical and systematic errors, are presented in Table 1. The efficiency for tagging uds events was about 35% and for tagging b events 23%.

4.1 Uncertainties in flavour composition

The systematic errors on the flavour compositions result from uncertainties in the detector modelling and imprecise knowledge of physics processes. For each source of uncertainty some aspect of the Monte Carlo was varied and the flavour composition of the uds-tag and b-tag event samples were recalculated. The difference between the flavour fractions calculated for each variation and the central value was taken as a systematic error on the determined flavour fractions.

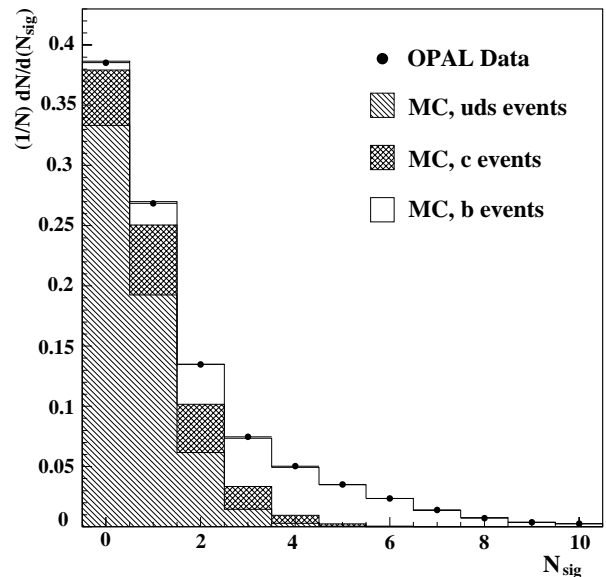


Fig. 1. Distribution of number of tracks per event (N_{sig}) with $b/\sigma_b > 2.5$. The points are data and the solid histogram is Monte Carlo. The Monte Carlo is also shown decomposed into contributions from uds, c and b quark events

Table 1. The fraction of uds, c and b quark events in each flavour-tagged event sample. The errors are the combined statistical and systematic errors

	uds fraction	charm fraction	bottom fraction
uds-tag	0.862 ± 0.010	0.119 ± 0.003	0.019 ± 0.011
c-tag	0.246 ± 0.005	0.548 ± 0.018	0.206 ± 0.017
b-tag	0.008 ± 0.002	0.028 ± 0.004	0.964 ± 0.019

4.1.1 Detector modelling uncertainties

Since the determination of the flavour fractions of the uds-tag and the b-tag event samples depends on Monte Carlo, this requires an accurate simulation of the detector resolution for charged tracks measured with the silicon micro-vertex detector. The simulation has been tuned to reproduce the tracking resolutions seen in data by studying the impact parameter distributions of tracks, as functions of track momentum, polar angle and the different sub-detectors contributing hits. This tuning procedure was affected by uncertainties in the radial alignment within the silicon micro-vertex detector, the efficiency for associating silicon hits to tracks and the modelling of known inefficient regions, and the overall track reconstruction efficiency. These uncertainties were evaluated according to the procedure given in [23] and their effect on the flavour fractions determined from Monte Carlo was calculated. In addition, the agreement between data and Monte Carlo in Fig. 1 was improved by degrading the resolution of impact parameters in the Monte Carlo simulation by 5%. This was done by applying a single multiplicative factor β to the difference between the reconstructed and true impact parameters. Figure 1 is shown with this smearing applied. To evaluate the sensitivity of the determined flavour frac-

Table 2. List of cuts used in the D^{*+} reconstruction. Note that both the scaled energy $x_{D^{*+}}$ and the mass difference ΔM are effective quantities, calculated from the reconstructed tracks only. The exact meaning of the different quantities is explained in the text

cut	3 prong	semileptonic	satellite	5 prong
$x_{D^{*+}}$	0.4–1.0	0.4–1.0	0.4–1.0	0.5–1.0
M_{D^0} [GeV]	1.79–1.94	1.20–1.80	1.41–1.77	1.79–1.94
ΔM [GeV]	0.142–0.149	0.140–0.162	0.141–0.151	0.142–0.149

tions to the tracking resolution the Monte Carlo smearing was removed.

4.1.2 Physics modelling uncertainties

The tagging efficiencies of the uds and b tags for the various quark flavours are also sensitive to various physics input parameters in the Monte Carlo simulation. The rate of gluon splitting to $c\bar{c}$ was varied in the range $(2.38 \pm 0.48) \times 10^{-2}$, based on the OPAL measurement [24], and the rate of gluon splitting to $b\bar{b}$ was varied in the range $(3.1 \pm 1.1) \times 10^{-3}$, based on theoretical expectation [25]. The error due to these two sources was negligible. The production fractions of the different weakly decaying b hadrons were varied according to the experimental uncertainties [26]. The production fractions of the weakly decaying c hadrons, the fragmentation of b and c quarks, and the charged decay multiplicities and lifetimes of b and c hadrons were varied according to the prescription given in [23]. The largest effect on the tag flavour fractions comes from the b hadron charged decay multiplicity. All these uncertainties, along with the uncertainties due to the detector modelling, were added in quadrature and are given as the errors on the flavour fraction shown in Table 1.

5 Selection of c quark events

Events having a high probability to have originated from $c\bar{c}$ were identified by the presence of a highly energetic D^{*+} meson³. These events will be referred to in the text below as the “c-tag” event sample. For the D^{*+} reconstruction and the determination of the flavour composition of the c-tag event sample the methods of a previous OPAL study have been used [27]. In brief, five D^{*+} decay modes were searched for:

$D^{*+} \rightarrow D^0\pi^+$	
↳ $K^-\pi^+$	“3 prong”
↳ $K^-\pi^+\pi^0$	“satellite”
↳ $K^-\pi^+\pi^-\pi^+$	“5 prong”
↳ $K^-e^+\nu_e$	“electron”
↳ $K^-\mu^+\nu_\mu$	“muon”

³ Throughout this paper charged conjugate modes are always implicitly included

No attempt was made to reconstruct the π^0 in the satellite channel, nor the neutrino direction or energy in the electron and muon channels. The last two channels are referred to as “semileptonic” channels in the following text. A number of tracks appropriate for the selected channel were combined to form a D^0 candidate and their invariant mass was calculated. Candidates were selected if the reconstructed mass lay within the expected range for that channel. After adding a further track as a possible pion from the D^{*+} decay, the combined mass was calculated and the candidate was selected if the mass difference $\Delta M = M_{D^{*+}} - M_{D^0}$ was within certain limits. Some of the D^{*+} selection criteria are given in Table 2.

To reduce the background in the c-tag event sample we required $x_{D^{*+}} > 0.4$, where $x_{D^{*+}} = E_{D^{*+}}^{calc}/E_{beam}$ is the scaled energy⁴ of the D^{*+} meson. For the 5-prong event selection we required $x_{D^{*+}} > 0.5$. This cut is effective in rejecting D^{*+} mesons which originate from cascade decays of B hadrons and from events where a gluon splits into a pair of charm quarks.

The distribution of ΔM for all five decay channels is presented in Fig. 2. The points with error bars are the signal candidates and the solid histograms are background estimator distributions constructed from data. The background estimator was constructed by choosing the candidate for the pion in the $D^{*+} \rightarrow D^0\pi^+$ decay from the opposite hemisphere relative to the rest of the decay products, reflecting it through the origin, and then using it in the calculation of the invariant mass.

A significant fraction of the sample of D^{*+} mesons were only partially reconstructed. These mesons produce an enhancement in the ΔM spectrum very similar to the true signal. Only a few of the events are present in the 3-prong sample. They are more important in the 5-prong tagged events where a clear tail is visible in the ΔM distribution for values above 0.145 GeV (see Fig. 2d). Since such events originate from D^{*+} decays, they can still be used in the analysis.

In all, 27 005 D^{*+} candidate events were selected and the background was estimated to be $11\,366 \pm 107$ events, where the error on the number of background events is statistical only. All of the LEP-1 data recorded by OPAL,

⁴ In this paper any reference to the scaled energy x of a D^{*+} candidate is to be understood as being the calculated energy of the D^{*+} , $E_{D^{*+}}^{calc}$, obtained from the reconstructed tracks, without correcting for missing or wrongly associated tracks, divided by the beam energy E_{beam}

OPAL

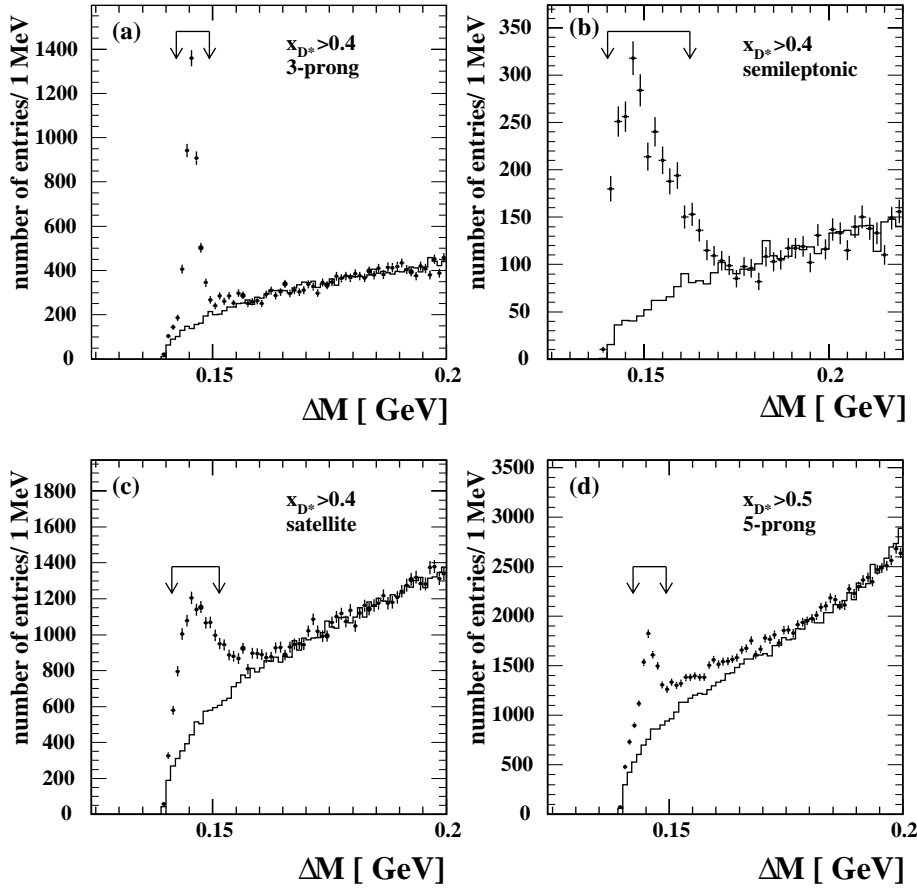


Fig. 2a–d. Distribution of the mass difference ΔM for four different D^{*+} decay channels: **a** 3-prong decay mode, **b** the two semileptonic modes combined, **c** the satellite decay mode, and **d** the 5-prong decay mode. The arrows indicate the selected signal regions. The points with error bars are the signal candidates and the solid histograms are the background estimator distributions

4.4 million events, was used for the D^{*+} event selection. The candidate events are composed of three components: genuine D^{*+} mesons from b events, genuine D^{*+} mesons from c events and combinatorial background which is a mixture of uds, c and b quark events. Genuine D^{*+} 's from uds quark events can only occur in events where a gluon splits into two heavy quarks. The possibility of D^{*+} 's from this source was neglected because these events are highly suppressed due to the high $x_{D^{*+}}$ cut. Using Monte Carlo simulation the total contribution of this source to the number of D^{*+} candidates was found to be $(0.2 \pm 0.1)\%$, where the error quoted is due to Monte Carlo statistics.

In Ref. [27] the fraction of genuine D^{*+} mesons originating from c events was determined by OPAL to be $f_c^{D^{*+}} = 0.774 \pm 0.023$, where the error is the combined statistical and systematic error. The fraction of genuine D^{*+} mesons from b events is given by $f_b^{D^{*+}} = 1 - f_c^{D^{*+}}$.

The fractions of uds, c and b quark events in the combinatorial background, as determined from Monte Carlo, were 0.584 ± 0.009 , 0.238 ± 0.009 and 0.178 ± 0.009 , respectively. The errors are a combination of statistical errors due to finite Monte Carlo statistics and a systematic error accounting for the overall quality of the background estimation procedure. Based on a Monte Carlo study [27] the background estimate was found to be accurate to within

1%, and an additional 1% error was therefore assigned to the number of background events. Since that study was flavour blind, a conservative approach was taken here where the entire error was assigned in turn to each flavour component in the combinatorial background.

The overall flavour composition of the c-tag event sample is presented in Table 1 along with the combined statistical and systematic errors. The efficiency for tagging c events was about 2.0%.

6 Event shape observables

For each flavour tagged event sample described above (uds-tag, c-tag and b-tag) the distributions of the event shape variables 1-Thrust ($1 - T$), Heavy Jet Mass scaled by the centre-of-mass energy (M_H/\sqrt{s}), Wide Jet Broadening (B_W), the y_{cut} at which an event changes from being a 2-jet event to being a 3-jet event (y_{23}) determined using the Durham jet finder and the C-parameter (C) were determined. The definitions for these observables are given in [17,28] and the references therein. These quantities were measured using all tracks and electromagnetic clusters which satisfied the selection criteria described in Sect. 3.

In order to extract the values of $\alpha_s^c/\alpha_s^{\text{uds}}$ and $\alpha_s^b/\alpha_s^{\text{uds}}$, the measured event shape distributions were fitted using a QCD analytic calculation [11]. Since the QCD calculation is only valid for event shape distributions determined from final-state partons, hadronization effects caused by the transformation of final-state partons into hadrons, which are experimentally accessible, must be taken into account. This was done by applying correction factors to the analytic predictions.

The measured event shape distributions must be corrected for experimental effects which distort them. These effects include finite detector resolution, initial-state photon radiation and biases introduced by the flavour tagging methods. In the text below describing the correction procedure the term *detector level* is used to refer to distributions determined using the measured tracks and electromagnetic clusters and *hadron level* to refer to these distributions corrected for detector resolution, initial state radiation and biases introduced by the flavour tagging methods. The comparisons between the measured distributions and the QCD predictions were performed at the hadron level.

The event shape variable Total Jet Broadening (B_T) [17] was initially considered to be included in this analysis. It was found, however, that for the distribution of B_T measured with b quark events, the size of the hadronization corrections were greater than 20% over the entire distribution. Therefore this variable was dropped from further consideration.

6.1 Correction procedure

In the first step the selected events were corrected for distortions caused by finite detector resolution using an unfolding matrix. The unfolding matrix was constructed using a Monte Carlo data sample including initial-state radiation, full detector simulation and subjected to the same event selection criteria that were applied to the data. The Monte Carlo events which pass the selection criteria were used to calculate a correction matrix $M^{q\text{-tag}}$. The element $M^{q\text{-tag}}(y_i, y_j)$ gives the probability that an event shape observable y measured at the detector level and located in bin i of its corresponding distribution, has migrated from bin j at the hadron level. A matrix was computed for each event shape observable and flavour-tagged event sample, “q-tag”, where q-tag was either uds-tag, c-tag or b-tag.

In the next step bin-by-bin corrections are used to correct the data for biases introduced by the flavour tagging methods, event acceptance and the effects of initial-state photon radiation. Defining $G^q(y_i)$ to be the number of events of flavour q in the untagged Monte Carlo sample and $H^{q\text{-tag}}(y_i)$ the number of events with the tag applied, the correction factor $K^{q\text{-tag}}(y_i)$ for the i -th bin is given by

$$K^{q\text{-tag}}(y_i) = \frac{f_{\text{uds}}^{q\text{-tag}} G^{\text{uds}}(y_i) + f_c^{q\text{-tag}} G^c(y_i) + f_b^{q\text{-tag}} G^b(y_i)}{H^{q\text{-tag}}(y_i)} \quad (1)$$

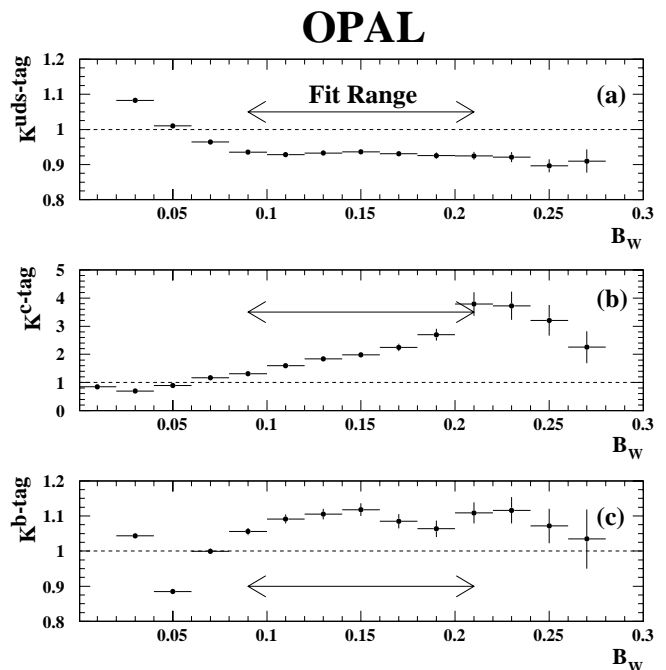


Fig. 3a–c. Bin-by-bin correction factors applied to the distribution of B_W for **a** the uds-tag event sample, **b** the c-tag event sample and **c** the b-tag event sample. The fit range for this observable (see Sect. 7) is indicated by the arrow on each figure

The factors $f_q^{q\text{-tag}}$, taken from Table 1, are the fractions of events of flavour q in each flavour-tagged event sample. The terms $G^q(y_i)$ are normalized to the total number of events of flavour q .

Figure 3 shows, as an example, the size of the bin-by-bin corrections $K^{q\text{-tag}}$ for the observable B_W measured using each flavour-tagged event sample. The size of the corrections for B_W were typical of the other event shape observables studied. One can see for the distributions measured with the uds-tag and b-tag event samples that, within the chosen fit range, the size of the corrections are about 10%. (An explanation of how the fit range was chosen is presented in the next section.) In contrast, the size of the corrections for the c-tag event sample were an order of magnitude larger. This is due to a kinematic bias introduced by requiring the events in the c-tag sample to contain a high- x D^{*+} meson.

The number of events in bin i corrected to the hadron level is given by

$$N^{q\text{-tag,cor}}(y_i) = K^{q\text{-tag}}(y_i) \sum_j M^{q\text{-tag}}(y_i, y_j) N^{q\text{-tag}}(y_j), \quad (2)$$

where $N^{q\text{-tag}}(y_j)$ is the uncorrected number of events in the j -th bin of the event shape distributions in question. This correction procedure does not depend on the values of α_s^{uds} , $\alpha_s^c/\alpha_s^{\text{uds}}$ or $\alpha_s^b/\alpha_s^{\text{uds}}$ in the Monte Carlo samples.

The resulting distributions normalized to the total hadronic cross section are given by

Table 3. The distribution of y_{23} , for each flavour-tagged event sample, corrected to the hadron level. The errors include statistical and experimental systematic uncertainties, added in quadrature

			$1/\sigma \, d\sigma/dy_{23}$							
y_{23}			uds-tag		c-tag			b-tag		
0.000	-	0.001	147.3	\pm 3.2	119.7	\pm 5.6	48.6	\pm 2.2		
0.001	-	0.002	156.0	\pm 2.0	166.9	\pm 4.0	177.4	\pm 3.0		
0.002	-	0.005	65.9	\pm 0.9	73.8	\pm 1.5	99.0	\pm 1.3		
0.005	-	0.010	26.4	\pm 0.2	26.8	\pm 0.8	27.1	\pm 0.4		
0.010	-	0.020	11.89	\pm 0.09	11.5	\pm 0.3	10.8	\pm 0.2		
0.020	-	0.030	6.06	\pm 0.09	5.8	\pm 0.3	5.6	\pm 0.1		
0.030	-	0.040	3.89	\pm 0.09	3.8	\pm 0.2	3.64	\pm 0.09		
0.040	-	0.050	2.76	\pm 0.07	2.7	\pm 0.1	2.60	\pm 0.08		
0.050	-	0.060	2.05	\pm 0.06	2.0	\pm 0.1	1.94	\pm 0.07		
0.060	-	0.080	1.42	\pm 0.04	1.42	\pm 0.07	1.35	\pm 0.04		
0.080	-	0.100	0.97	\pm 0.03	0.94	\pm 0.06	0.92	\pm 0.03		
0.100	-	0.120	0.68	\pm 0.02	0.66	\pm 0.05	0.67	\pm 0.03		
0.120	-	0.140	0.51	\pm 0.02	0.51	\pm 0.04	0.49	\pm 0.02		
0.140	-	0.170	0.36	\pm 0.01	0.37	\pm 0.05	0.35	\pm 0.02		
0.170	-	0.200	0.24	\pm 0.01	0.26	\pm 0.04	0.24	\pm 0.01		

Table 4. The distribution of $1 - T$, for each flavour-tagged event sample, corrected to the hadron level. The errors include statistical and experimental systematic uncertainties, added in quadrature

			$1/\sigma \, d\sigma/d(1 - T)$							
$1 - T$			uds-tag		c-tag			b-tag		
0.00	-	0.02	7.61	\pm 0.08	7.1	\pm 0.2	5.9	\pm 0.2		
0.02	-	0.04	15.61	\pm 0.17	16.1	\pm 0.2	17.0	\pm 0.2		
0.04	-	0.06	8.27	\pm 0.04	8.4	\pm 0.2	8.5	\pm 0.1		
0.06	-	0.08	5.07	\pm 0.06	5.1	\pm 0.1	5.2	\pm 0.1		
0.08	-	0.10	3.42	\pm 0.05	3.5	\pm 0.1	3.42	\pm 0.10		
0.10	-	0.12	2.46	\pm 0.05	2.5	\pm 0.1	2.47	\pm 0.07		
0.12	-	0.14	1.81	\pm 0.04	1.7	\pm 0.1	1.78	\pm 0.05		
0.14	-	0.16	1.36	\pm 0.03	1.31	\pm 0.09	1.38	\pm 0.05		
0.16	-	0.18	1.05	\pm 0.02	1.00	\pm 0.06	1.04	\pm 0.03		
0.18	-	0.20	0.83	\pm 0.02	0.80	\pm 0.05	0.82	\pm 0.03		
0.20	-	0.22	0.65	\pm 0.02	0.67	\pm 0.09	0.65	\pm 0.02		
0.22	-	0.24	0.52	\pm 0.01	0.52	\pm 0.07	0.51	\pm 0.02		
0.24	-	0.26	0.41	\pm 0.01	0.43	\pm 0.07	0.41	\pm 0.02		
0.26	-	0.28	0.32	\pm 0.01	0.33	\pm 0.05	0.33	\pm 0.02		
0.28	-	0.30	0.237	\pm 0.008	0.24	\pm 0.04	0.25	\pm 0.01		
0.30	-	0.32	0.177	\pm 0.007	0.18	\pm 0.04	0.20	\pm 0.01		
0.32	-	0.34	0.113	\pm 0.005	0.10	\pm 0.05	0.12	\pm 0.01		
0.34	-	0.36	0.058	\pm 0.004	0.04	\pm 0.02	0.054	\pm 0.006		
0.36	-	0.38	0.022	\pm 0.002	0.02	\pm 0.02	0.021	\pm 0.004		

Table 5. The distribution of M_H/\sqrt{s} , for each flavour-tagged event sample, corrected to the hadron level. The errors include statistical and experimental systematic uncertainties, added in quadrature

M_H/\sqrt{s}	$1/\sigma \, d\sigma/d(M_H/\sqrt{s})$										
	uds-tag			c-tag			b-tag				
0.04	-	0.08	0.14	±	0.01	0.10	±	0.01	0.014	±	0.003
0.08	-	0.12	2.51	±	0.07	2.37	±	0.09	2.08	±	0.11
0.12	-	0.16	6.54	±	0.06	6.65	±	0.13	6.98	±	0.10
0.16	-	0.20	5.07	±	0.02	5.19	±	0.14	5.17	±	0.06
0.20	-	0.24	3.39	±	0.04	3.40	±	0.07	3.40	±	0.08
0.24	-	0.28	2.38	±	0.03	2.35	±	0.07	2.42	±	0.07
0.28	-	0.32	1.71	±	0.03	1.68	±	0.09	1.72	±	0.04
0.32	-	0.36	1.21	±	0.02	1.19	±	0.05	1.20	±	0.03
0.36	-	0.40	0.84	±	0.02	0.83	±	0.04	0.83	±	0.03
0.40	-	0.44	0.56	±	0.01	0.57	±	0.04	0.55	±	0.02
0.44	-	0.48	0.35	±	0.01	0.37	±	0.04	0.35	±	0.01
0.48	-	0.52	0.198	±	0.007	0.21	±	0.02	0.197	±	0.008
0.52	-	0.56	0.078	±	0.003	0.07	±	0.02	0.076	±	0.006
0.56	-	0.60	0.012	±	0.001	0.01	±	0.01	0.011	±	0.002

Table 6. The distribution of B_W , for each flavour-tagged event sample, corrected to the hadron level. The errors include statistical and experimental systematic uncertainties, added in quadrature

B_W	$1/\sigma \, d\sigma/dB_W$										
	uds-tag			c-tag			b-tag				
0.00	-	0.02	0.90	±	0.08	0.54	±	0.06	0.02	±	0.01
0.02	-	0.04	14.06	±	0.13	13.8	±	0.4	12.6	±	0.2
0.04	-	0.06	11.09	±	0.10	11.8	±	0.3	13.7	±	0.2
0.06	-	0.08	7.32	±	0.06	7.4	±	0.2	7.4	±	0.1
0.08	-	0.10	5.03	±	0.04	4.1	±	0.1	5.02	±	0.10
0.10	-	0.12	3.56	±	0.04	3.4	±	0.1	3.51	±	0.07
0.12	-	0.14	2.57	±	0.04	2.5	±	0.1	2.51	±	0.06
0.14	-	0.16	1.85	±	0.04	1.82	±	0.09	1.78	±	0.06
0.16	-	0.18	1.34	±	0.03	1.34	±	0.08	1.29	±	0.05
0.18	-	0.20	0.94	±	0.03	0.94	±	0.08	0.90	±	0.03
0.20	-	0.22	0.64	±	0.02	0.68	±	0.08	0.63	±	0.02
0.22	-	0.24	0.41	±	0.02	0.46	±	0.08	0.40	±	0.02
0.24	-	0.26	0.22	±	0.01	0.22	±	0.04	0.21	±	0.01
0.26	-	0.28	0.071	±	0.004	0.07	±	0.02	0.065	±	0.008

$$\left(\frac{1}{\sigma_{tot}} \frac{d\sigma}{dy} \right)^{q-tag,cor} = \frac{1}{\Delta y_i \cdot \sum_j N^{q-tag,cor}(y_j)} N^{q-tag,cor}(y_i), \quad (3)$$

where Δy_i is the width of the i -th bin and y corresponds to one of the five event shapes studied. The distributions of each observable, corrected to the hadron level, are presented in Tables 3 through 7. The given errors include statistical and experimental systematic uncertainties, added in quadrature.

7 Fit procedure

The value of α_s^{uds} and the ratios $\alpha_s^c/\alpha_s^{\text{uds}}$ and $\alpha_s^b/\alpha_s^{\text{uds}}$ were determined by simultaneously fitting theoretical predictions for a particular event shape observable to three hadron-level event shape distributions: one determined with the uds-tag event sample, one with the c-tag event sample and one with the b-tag event sample. The theoretical predictions were given by a linear combination of the theoretical predictions for each of the three tagged flavours:

Table 7. The distribution of C , for each flavour-tagged event sample, corrected to the hadron level. The errors include statistical and experimental systematic uncertainties, added in quadrature

C	$1/\sigma \, d\sigma/dC$										
	uds-tag			c-tag			b-tag				
0.00	-	0.03	0.08	±	0.03	0.05	±	0.02	0.003	±	0.002
0.03	-	0.06	1.01	±	0.08	0.78	±	0.08	0.22	±	0.03
0.06	-	0.09	3.13	±	0.03	2.90	±	0.11	2.28	±	0.12
0.09	-	0.12	4.26	±	0.03	4.31	±	0.10	4.61	±	0.07
0.12	-	0.14	3.92	±	0.03	4.10	±	0.10	4.55	±	0.06
0.14	-	0.16	3.35	±	0.04	3.50	±	0.09	3.79	±	0.05
0.16	-	0.18	2.84	±	0.04	2.97	±	0.08	3.14	±	0.05
0.18	-	0.20	2.45	±	0.03	2.55	±	0.07	2.63	±	0.05
0.20	-	0.22	2.15	±	0.02	2.23	±	0.07	2.28	±	0.05
0.22	-	0.24	1.94	±	0.02	1.98	±	0.07	2.03	±	0.05
0.24	-	0.26	1.73	±	0.03	1.77	±	0.07	1.79	±	0.04
0.26	-	0.28	1.57	±	0.03	1.62	±	0.08	1.61	±	0.04
0.28	-	0.30	1.42	±	0.02	1.46	±	0.07	1.46	±	0.03
0.30	-	0.32	1.29	±	0.02	1.32	±	0.07	1.33	±	0.03
0.32	-	0.34	1.19	±	0.02	1.19	±	0.05	1.22	±	0.03
0.34	-	0.36	1.09	±	0.02	1.07	±	0.05	1.10	±	0.04
0.36	-	0.38	1.00	±	0.02	0.98	±	0.05	1.00	±	0.03
0.38	-	0.40	0.93	±	0.02	0.93	±	0.06	0.95	±	0.04
0.40	-	0.42	0.86	±	0.02	0.84	±	0.06	0.87	±	0.03
0.42	-	0.44	0.81	±	0.02	0.81	±	0.05	0.83	±	0.03
0.44	-	0.48	0.73	±	0.02	0.72	±	0.04	0.74	±	0.02
0.48	-	0.52	0.63	±	0.01	0.62	±	0.03	0.62	±	0.02
0.52	-	0.58	0.54	±	0.01	0.53	±	0.03	0.53	±	0.01
0.58	-	0.64	0.44	±	0.01	0.43	±	0.02	0.44	±	0.01
0.64	-	0.70	0.365	±	0.008	0.36	±	0.02	0.36	±	0.01
0.70	-	0.76	0.315	±	0.008	0.32	±	0.03	0.32	±	0.01
0.76	-	0.88	0.160	±	0.004	0.16	±	0.02	0.169	±	0.004
0.88	-	1.00	0.014	±	0.002	0.012	±	0.002	0.012	±	0.001

$$\begin{aligned}
\left(\frac{1}{\sigma_{tot}} \frac{d\sigma}{dy}\right)^{q-tag,th} &= f_{uds}^{q-tag} R(y)^{uds} \left(\frac{1}{\sigma_{tot}} \frac{d\sigma}{dy}\right)^{uds,th} \\
&+ f_c^{q-tag} R(y)^c \left(\frac{1}{\sigma_{tot}} \frac{d\sigma}{dy}\right)^{c,th} \\
&+ f_b^{q-tag} R(y)^b \left(\frac{1}{\sigma_{tot}} \frac{d\sigma}{dy}\right)^{b,th} . \quad (4)
\end{aligned}$$

The coefficients f_q^{q-tag} are the flavour fractions given in Table 1 and $(1/\sigma_{tot} \cdot d\sigma/dy)^{uds,th}$, $(1/\sigma_{tot} \cdot d\sigma/dy)^{c,th}$ and $(1/\sigma_{tot} \cdot d\sigma/dy)^{b,th}$ are the theoretical predictions for an event shape observable y measured with a sample of uds, c and b quark events, respectively. The factors $R(y)^q$ correct the theoretical prediction for a particular tagged flavour q for hadronization effects so that the theoretical predictions, valid for final state partons, can be compared directly with the measured distributions corrected to the hadron level.

The hadronization correction factors $R(y)^q$ were computed from JETSET 7.4 using the parton shower option by taking the ratio of an event shape distribution at the hadron level to the same distribution at the parton level. Here the parton level is defined by the cut-off Q_0 of the QCD shower in JETSET which is set to 1.9 GeV [19]. After the termination of the parton shower the partons are transformed into hadrons using string hadronization [29]. For this process we choose a hybrid scheme for the longitudinal fragmentation function where light quarks are treated with the symmetric Lund fragmentation function and charm and bottom quarks according to the model of Peterson et al. [20]. The c and b quark masses in JETSET were set to their default values of 1.35 GeV and 5.0 GeV, respectively.

In (4), the differential cross section of a generic observable y , for massless quarks, normalized to the total hadronic cross section is given by [30]

$$\begin{aligned}
 & \left(\frac{1}{\sigma_{tot}} \frac{d\sigma}{dy} \right)^{uds,th} \\
 &= \frac{dA^{uds}}{dy} \left(\frac{\alpha_s^{uds}(\mu)}{2\pi} \right) \\
 &+ \left((2\pi\beta_0 \log(x_\mu^2) - 2) \frac{dA^{uds}}{dy} + \frac{dB^{uds}}{dy} \right) \\
 &\times \left(\frac{\alpha_s^{uds}(\mu)}{2\pi} \right)^2. \tag{5}
 \end{aligned}$$

The coefficients dA^{uds}/dy and dB^{uds}/dy are the $\mathcal{O}(\alpha_s)$ and $\mathcal{O}(\alpha_s^2)$ QCD coefficients, respectively, σ_{tot} is the one-loop cross section for the process $e^+e^- \rightarrow$ hadrons and β_0 is the coefficient of the QCD beta function for one-loop [26]. The renormalization scale μ can be related to the e^+e^- centre-of-mass energy by

$$\mu = x_\mu \cdot E_{cm}, \tag{6}$$

where x_μ is the renormalization scale factor. The coefficients dA^{uds}/dy and dB^{uds}/dy were obtained for each event shape observable by integrating the $\mathcal{O}(\alpha_s^2)$ matrix elements in [30]. In (5), in addition to the approximation of massless quarks, the simplifying assumption was made that α_s is the same for up, down and strange quarks.

The terms $(1/\sigma_{tot} \cdot d\sigma/dy)^{c,th}$ and $(1/\sigma_{tot} \cdot d\sigma/dy)^{b,th}$ in (4) were both given by an $\mathcal{O}(\alpha_s^2)$ expression for massive quarks. This expression has only recently been made available [11]. The result of this calculation was implemented in a FORTRAN program named ZBB4 [31] analogous to the program EVENT [32] which was used to integrate the $\mathcal{O}(\alpha_s^2)$ matrix elements of the massless calculation. ZBB4 was run separately for c quark and b quark events in order to calculate the $\mathcal{O}(\alpha_s)$ and $\mathcal{O}(\alpha_s^2)$ coefficients for the massive calculation. This calculation was performed in the pole mass scheme and the c and b quark pole masses were set to 1.35 GeV and 5.0 GeV, respectively.

The differential cross section of a generic observable y , for massive quarks, normalized to the total hadronic cross section is given by [31]

$$\begin{aligned}
 & \left(\frac{1}{\sigma_{tot}} \frac{d\sigma}{dy} \right)^{Q,th} \\
 &= \frac{dA^Q}{dy} \left(\frac{\alpha_s^Q(\mu)}{2\pi} \right) \\
 &+ \left(\left(2\pi\beta_0 \log(x_\mu^2) - \frac{2}{3} \log\left(\frac{\mu}{m_Q}\right) - 2 \right) \frac{dA^Q}{dy} + \frac{dB^Q}{dy} \right) \\
 &\times \left(\frac{\alpha_s^Q(\mu)}{2\pi} \right)^2 \tag{7}
 \end{aligned}$$

where Q is either c or b and m_Q is the energy scale corresponding to the heavy quark pole mass.

When performing the fit using (4) we make the substitution $\alpha_s^c = \alpha_s^{uds} \cdot \alpha_s^c / \alpha_s^{uds}$ and $\alpha_s^b = \alpha_s^{uds} \cdot \alpha_s^b / \alpha_s^{uds}$. This substitution enables α_s^{uds} , $\alpha_s^c / \alpha_s^{uds}$ and $\alpha_s^b / \alpha_s^{uds}$ to be determined directly as free parameters in the fit and allows correlations between these variables to be properly taken

OPAL

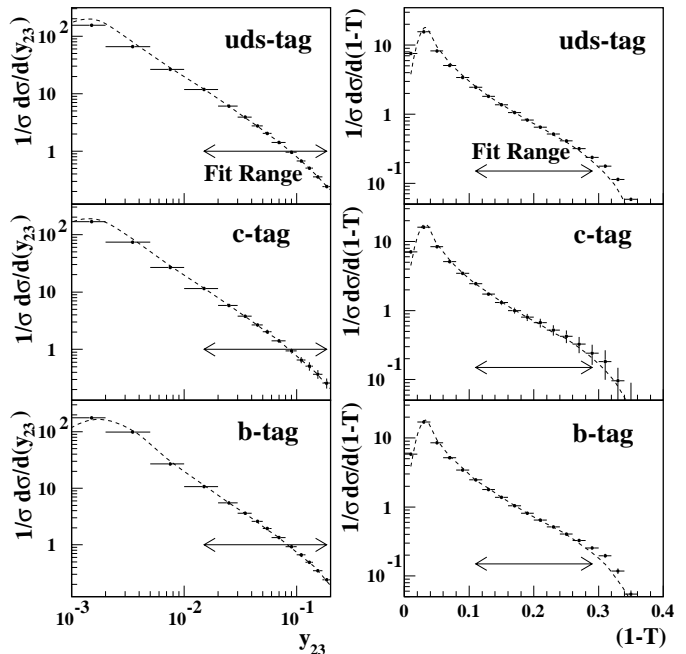


Fig. 4. The points with error bars are the distributions of y_{23} and $1-T$ measured in three flavour-tagged event samples (uds-tag, c-tag and b-tag) corrected to the hadron level. The curves show the result of simultaneous fits of $\mathcal{O}(\alpha_s^2)$ calculations to the distributions measured in each flavour-tagged event sample. The renormalization scale x_μ was fixed equal to one. The fit range for each distribution is indicated by the arrows

into account. In tests with Monte Carlo events it was verified that this fitting procedure was sensitive to changes in α_s for c and b quarks with respect to uds quarks.

The fit ranges for each observable were determined by the range of y where the parton to hadron level corrections were generally below 10% and the resulting $\chi^2/\text{d.o.f.}$ remained small (~ 5 for B_W and $\sim 2-3$ for the rest). The remaining variations of the fit results due to the choice of the fit ranges were taken as systematic uncertainties. It was also checked that within the fit range the $\mathcal{O}(\alpha_s^2)$ calculation and the JETSET parton shower model were in agreement with each other. The fit ranges used for this analysis are slightly smaller than the fit ranges used in previous OPAL studies [17, 28] which used $\mathcal{O}(\alpha_s^2)$ calculations in fits to global event shapes. This is because the hadronization corrections for distributions of event shape variables calculated with b quark events are generally larger than the corrections for distributions calculated with an inclusive event sample. Consequently, the range of the distribution in which the corrections are below 10% is smaller.

The fit ranges, and the results of the χ^2 fits with $x_\mu = 1$ are shown in Table 8. The values for α_s^{uds} obtained appear large when compared with α_s measurements performed using resummed NLO calculations [17, 33]. This is characteristic of α_s values obtained from fits to global event shapes using fix order QCD calculations and the renormalization scale factor $x_\mu = 1$. [28, 34].

Table 8. Results of the χ^2 fits with the renormalization scale factor fixed: $x_\mu = 1$. The errors are statistical

Event shape	Fit Range	α_s^{uds}	$\alpha_s^c/\alpha_s^{\text{uds}}$	$\alpha_s^b/\alpha_s^{\text{uds}}$	$\chi^2/\text{d.o.f.}$
y_{23}	0.015 – 0.185	0.1263 ± 0.0006	1.017 ± 0.034	1.004 ± 0.007	42.1/30
$1 - T$	0.11 – 0.29	0.1451 ± 0.0011	0.967 ± 0.055	0.993 ± 0.011	60.3/27
M_H	0.26 – 0.42	0.1344 ± 0.0009	1.004 ± 0.047	1.008 ± 0.009	29.6/12
B_W	0.09 – 0.21	0.1313 ± 0.0007	1.006 ± 0.039	1.003 ± 0.008	79.8/18
C	0.35 – 0.67	0.1424 ± 0.0010	0.986 ± 0.050	0.982 ± 0.011	39.0/24

Table 9. Results of the χ^2 fits with the renormalization scale factor x_μ as a free parameter. The errors are statistical. The fit ranges are given in Table 8

Event shape	α_s^{uds}	$\alpha_s^c/\alpha_s^{\text{uds}}$	$\alpha_s^b/\alpha_s^{\text{uds}}$	x_μ	$\chi^2/\text{d.o.f.}$
y_{23}	0.1188 ± 0.0010	1.008 ± 0.030	0.991 ± 0.006	0.266 ± 0.066	29.4/29
$1 - T$	0.1163 ± 0.0017	0.963 ± 0.036	0.979 ± 0.007	0.083 ± 0.017	13.6/26
M_H	0.1195 ± 0.0006	0.990 ± 0.037	0.992 ± 0.008	0.088 ± 0.021	13.7/11
B_W	0.1191 ± 0.0006	0.995 ± 0.033	0.995 ± 0.007	0.086 ± 0.011	31.3/17
C	0.1125 ± 0.0014	0.973 ± 0.032	0.984 ± 0.010	0.041 ± 0.014	26.1/23

Table 10. Systematic errors on the ratio $\alpha_s^c/\alpha_s^{\text{uds}}$. Where a signed value is quoted, this indicates the direction in which the ratio changed with respect to the default analysis when a certain feature of the analysis was changed. See the text for a description of the systematic errors

Event shape	y_{23}	$1 - T$	M_H/\sqrt{s}	B_W	C	Mean
$\alpha_s^c/\alpha_s^{\text{uds}}$	1.013	0.965	0.997	1.001	0.979	0.997
Statistical error	± 0.032	± 0.045	± 0.042	± 0.036	± 0.041	± 0.038
Flavour composition	± 0.002	± 0.002	± 0.001	± 0.001	± 0.002	± 0.001
Clusters only	+0.015	+0.011	+0.014	+0.014	+0.033	+0.017
Tracks only	+0.009	+0.012	+0.037	+0.006	± 0.001	+0.012
$\cos\theta_{\text{Th}} < 0.7$	+0.005	-0.008	+0.027	+0.010	+0.022	+0.011
$N_{ch} \geq 7$	< 0.001	+0.001	+0.001	+0.001	+0.001	+0.001
Fit range	± 0.008	± 0.016	± 0.010	± 0.013	± 0.003	± 0.004
$x_{D^{*+}}$ range	± 0.009	± 0.045	± 0.020	± 0.008	± 0.037	± 0.019
Experimental syst.	± 0.022	± 0.051	± 0.053	± 0.024	± 0.055	± 0.030
Lund frag. b	± 0.003	± 0.001	± 0.002	± 0.002	± 0.001	± 0.001
Peterson frag. ϵ_c	± 0.010	± 0.003	± 0.002	± 0.001	± 0.003	± 0.003
Peterson frag. ϵ_b	± 0.005	± 0.004	± 0.004	± 0.004	± 0.003	± 0.004
Q_0	± 0.006	± 0.001	< 0.001	± 0.003	± 0.003	± 0.003
σ_q	± 0.004	± 0.003	± 0.014	< 0.001	± 0.005	± 0.002
Scale uncertainty	± 0.004	± 0.002	± 0.007	± 0.005	± 0.006	± 0.007
ARIADNE	-0.008	< 0.001	-0.001	-0.004	-0.001	-0.004
c quark mass	± 0.008	± 0.005	< 0.001	± 0.005	± 0.006	± 0.005
b quark mass	± 0.001	< 0.001	< 0.001	± 0.001	< 0.001	< 0.001
Theoretical error	± 0.018	± 0.008	± 0.016	± 0.010	± 0.011	± 0.012
Total error	± 0.043	± 0.069	± 0.070	± 0.044	± 0.069	± 0.050

Table 11. Systematic errors on the ratio $\alpha_s^b/\alpha_s^{uds}$. Where a signed value is quoted, this indicates the direction in which the ratio changed with respect to the default analysis when a certain feature of the analysis was changed. See the text for a description of the systematic errors

Event shape	y_{23}	$1 - T$	M_H/\sqrt{s}	B_W	C	Mean
$\alpha_s^b/\alpha_s^{uds}$	0.997	0.986	1.000	0.999	0.983	0.993
Statistical error	± 0.007	± 0.009	± 0.008	± 0.008	± 0.010	± 0.008
Flavour composition	± 0.001	± 0.001	< 0.001	< 0.001	± 0.001	< 0.001
Clusters only	-0.004	$+0.001$	$+0.001$	$+0.001$	± 0.001	< 0.001
Tracks only	-0.006	$+0.002$	$+0.003$	$+0.001$	-0.001	-0.001
$\cos\theta_{Th} < 0.7$	< 0.001	-0.001	$+0.002$	$+0.001$	$+0.002$	$+0.001$
$N_{ch} \geq 7$	< 0.001	< 0.001	< 0.001	< 0.001	< 0.001	< 0.001
Fit range	± 0.016	± 0.008	± 0.009	± 0.003	± 0.003	± 0.005
$x_{D^{*+}}$ range	± 0.001	± 0.004	± 0.002	± 0.002	± 0.003	± 0.002
Experimental syst.	± 0.017	± 0.010	± 0.011	± 0.004	± 0.005	± 0.006
Lund frag. b	± 0.001	± 0.005	± 0.003	± 0.001	± 0.005	± 0.001
Peterson frag. ϵ_c	± 0.003	± 0.007	± 0.005	± 0.002	± 0.001	± 0.003
Peterson frag. ϵ_b	± 0.004	± 0.004	± 0.003	± 0.001	± 0.004	± 0.002
Q_0	± 0.004	± 0.008	± 0.003	± 0.003	± 0.005	± 0.003
σ_q	± 0.003	± 0.009	± 0.005	< 0.001	± 0.001	± 0.001
Scale uncertainty	± 0.006	± 0.007	± 0.008	± 0.004	± 0.001	± 0.005
ARIADNE	$+0.004$	-0.001	-0.001	$+0.008$	-0.002	$+0.002$
c quark mass	< 0.001	< 0.001	< 0.001	< 0.001	< 0.001	< 0.001
b quark mass	± 0.012	± 0.008	± 0.005	± 0.010	± 0.010	± 0.008
Theoretical error	± 0.016	± 0.018	± 0.013	± 0.014	± 0.013	± 0.011
Total error	± 0.025	± 0.022	± 0.019	± 0.016	± 0.017	± 0.014

To estimate the error in our results due to the choice of the renormalization scale we adopted a method used in another OPAL analysis [28] which used $\mathcal{O}(\alpha_s^2)$ fits to global event shapes. We performed fits with x_μ fixed equal one, and fits in which x_μ was an additional free parameter. The average of the two results is taken as our main result, and half their difference as the ‘‘scale uncertainty’’. The result of fits with x_μ as a free parameter are presented in Table 9. One sees that the values of α_s^{uds} decrease for all event shapes and that the values of $\chi^2/\text{d.o.f.}$ show a significant improvement. This strong scale dependence is typical of determinations of α_s where fixed order calculations are used. It was checked that the values of α_s^{uds} determined here were consistent with previous OPAL measurements of α_s [17, 28]. The possibility of a different scale dependence for heavy quark events, due to mass effects present in higher order terms, was investigated by introducing a separate x_μ parameter for each quark flavour. The effect was found to be negligible within the statistical precision of the measurement.

In Figs. 4 through 6 the results of fits with $x_\mu = 1$ are plotted along with the measured distributions corrected to the hadron level. The fit ranges used are indicated by the arrow on each figure. It can be seen that within the fit ranges the agreement between the fit results and the data

are good. In Fig. 4 one sees a small disagreement between the fit results and the data for values of $1 - T > 0.25$. When the fits to $1 - T$ were repeated with x_μ as a free parameter, the agreement between the fit results and data were good over the entire fit range.

8 Systematic uncertainties

The main result was obtained using the default selection and correction procedure described above. The systematic uncertainties were divided into two groups: experimental and theoretical uncertainties. Each uncertainty was estimated by modifying details of the event selection and correction procedure and repeating the analysis. The difference between the results obtained with the standard analysis and the results obtained with the analysis corresponding to each variation were taken (unless otherwise noted) as symmetric systematic errors. In the case where a parameter was varied above or below its nominal value, the largest deviation from the main result was taken as a symmetric systematic error associated with that parameter. Finally, the systematic errors for each type of variation were added in quadrature. The systematic uncertainties investigated are described below and the effects they

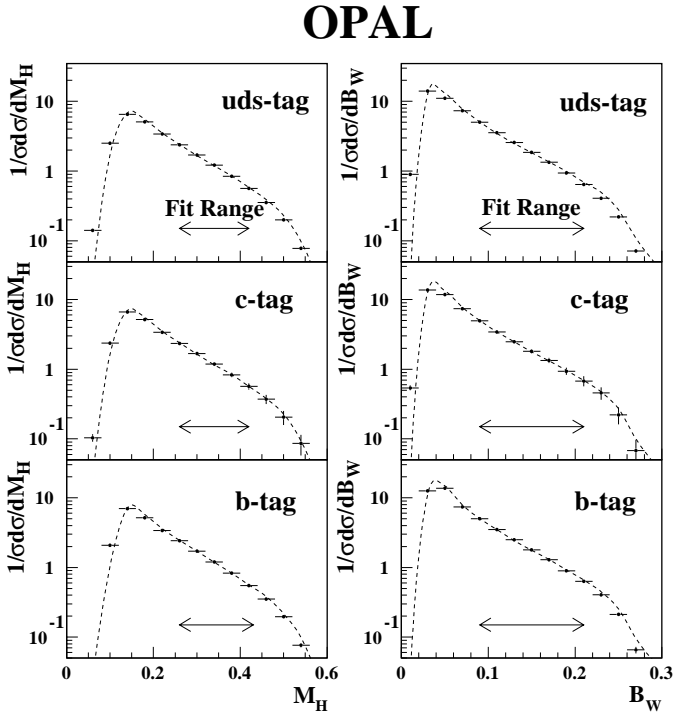


Fig. 5. The points with error bars are the distributions of M_H and B_W measured in three flavour-tagged event samples (uds-tag, c-tag and b-tag) corrected to the hadron level. The curves show the result of simultaneous fits of $\mathcal{O}(\alpha_s^2)$ calculations to the distributions measured in each flavour-tagged event sample. The renormalization scale x_μ was fixed equal to one. The fit range for each distribution is indicated by the arrows

had on the ratios $\alpha_s^c/\alpha_s^{\text{uds}}$ and $\alpha_s^b/\alpha_s^{\text{uds}}$ are presented in Tables 10 and 11.

8.1 Experimental systematic uncertainties

- The error due to the uncertainty on the flavour composition of the flavour-tagged event samples was evaluated by varying the flavour fractions in Table 1 within their errors.
- For the central result event shape observables were measured using all charged tracks and electromagnetic clusters. To evaluate the relative response of the central tracking and the electromagnetic calorimeter the measurements were performed again using electromagnetic clusters only and charged tracks only.
- The homogeneity of the response of the detector in the endcap region was checked by restricting the analysis to the barrel region of the detector, requiring the thrust axis of accepted events to lie within the range $|\cos\theta_{\text{Th}}| < 0.7$. This only modifies event shape distributions measured with the c-tag event sample because the uds-tag and b-tag event samples are already restricted to the barrel region.
- The minimum number of accepted charged tracks was increased from 5 to 7 in order to further suppress background from $\tau^+\tau^-$ events and two-photon interactions.

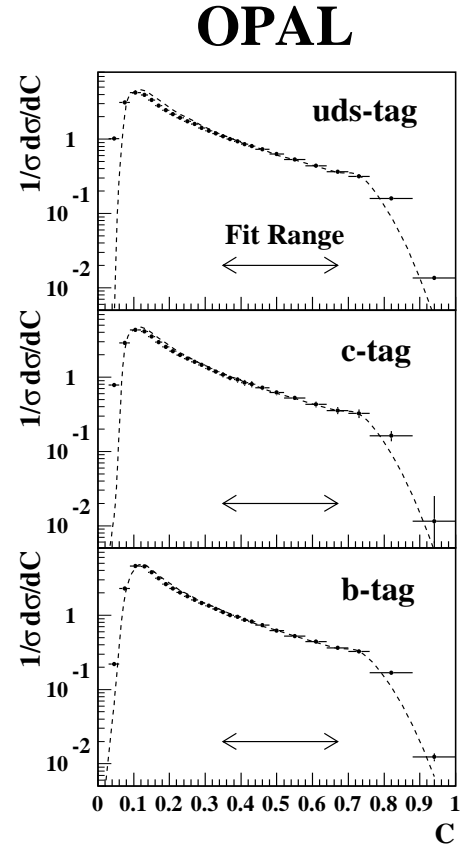


Fig. 6. The points with error bars are the distribution of the C parameter measured in three flavour-tagged event samples (uds-tag, c-tag and b-tag) corrected to the hadron level. The curves show the result of simultaneous fits of $\mathcal{O}(\alpha_s^2)$ calculations to the distributions measured in each flavour-tagged event sample. The renormalization scale x_μ was fixed equal to one. The fit range for each distribution is indicated by the arrows

- The dependence of the result on the chosen fit range was evaluated by adding or subtracting one bin from the lower and upper end of the fit range. Out of the four possible variations, the one which produced the largest change in the fit result was used to calculate the systematic error. In all cases, this was when one bin was added to the lower end of the fit range, thus extending the fit further into the two jet region.
- In the charm event selection the requirement that $x_{D^{*+}} > 0.4$ leads to a large kinematic bias in the c-tag event sample. The uncertainty due to this aspect of the D^{*+} selection was evaluated by varying the $x_{D^{*+}}$ cut between 0.3 and 0.5.

8.2 Theoretical systematic uncertainties

- The fragmentation of the final-state partons into hadrons was modelled by JETSET where the longitudinal fragmentation function for light quarks was treated by the symmetric Lund model and for heavy quarks by the model of Peterson et al [20]. The parameters for each model were determined from a fit

to OPAL data on global event shapes [19]. This fit yielded a value of $b = 0.52 \pm 0.04$ (PARJ(42)) for the Lund model and $\epsilon_c = 0.031 \pm 0.011$ (PARJ(54)) and $\epsilon_b = 0.0038 \pm 0.0010$ (PARJ(55)) for the Peterson model. To evaluate the systematic error due to uncertainties in the JETSET hadronization model these parameters were varied independently within one standard deviation of their optimised values.

- In JETSET, the parameter Q_0 (PARJ(82)) is the virtuality cut-off of partons. It determines the boundary between the perturbative QCD and hadronization phases and is essentially arbitrary. The optimum value to describe the OPAL data was determined to be $Q_0 = (1.90 \pm 0.50)$ GeV [19]. This parameter was varied within one standard deviation of its optimised value.
- The width of the transverse momentum distributions of quarks and antiquarks produced in the fragmentation process is determined by the parameter $\sigma_q = (0.40 \pm 0.03)$ GeV (PARJ(21)). This parameter was varied within one standard deviation of its optimum value.
- The renormalization scale uncertainty was estimated by performing fits with x_μ fixed equal one, and fits in which x_μ is an additional free parameter. The average of the two results is taken as our main result, and half their difference as the scale uncertainty.
- To evaluate the dependence of this analysis on the choice of using JETSET to calculate the hadronization corrections, the analysis was repeated using ARIADNE 4.08 [35] instead of JETSET. The ARIADNE parton shower is based upon a colour dipole model and provides an alternative to the Lund parton shower model in JETSET. ARIADNE employs the same fragmentation model as JETSET for the subsequent hadronization. The difference between the results using JETSET hadronization corrections and ARIADNE corrections were used as an estimate of this systematic error.

There was poor agreement, at the detector level, between HERWIG 5.9 [36] and the event shape distributions measured with the b-tag event sample. Therefore HERWIG was not used to evaluate this systematic error. OPAL has not tuned HERWIG to reproduce b-quark events.

- The error due to uncertainties in the c and b quark masses was evaluated by varying the quark masses in the ranges given in [26] and repeating the integration of the matrix elements corresponding to massive quarks for each variation. The value for the b quark pole mass was varied from 4.5 to 5.5 GeV/ c^2 ; the c quark pole mass was varied from 1.2 to 1.9 GeV/ c^2 .

9 Results

The results of the χ^2 fits to determine $\alpha_s^c/\alpha_s^{\text{uds}}$ and $\alpha_s^b/\alpha_s^{\text{uds}}$ for each of the event shape observables studied are presented in Tables 10 and 11 and summarised in Fig. 7. The values quoted are the average of fits with $x_\mu = 1$ and with x_μ as a free parameter. The top half

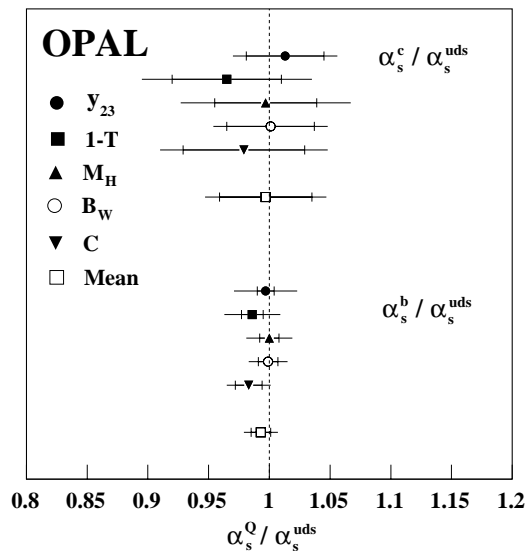


Fig. 7. The ratios $\alpha_s^c/\alpha_s^{\text{uds}}$ and $\alpha_s^b/\alpha_s^{\text{uds}}$ determined for each of the event shapes studied. The weighted mean of the results derived for the five event shape observables is also shown. The inner error bar represents the statistical error while the full error bar represents the statistical error and the systematic error added in quadrature

of the Figure 7 shows the result of determining $\alpha_s^c/\alpha_s^{\text{uds}}$ and the lower half $\alpha_s^b/\alpha_s^{\text{uds}}$. The vertical bars on the error bars show the size of the statistical error and the full error bar is the total error, which is the sum of the statistical, experimental systematic and theoretical errors added in quadrature. Also shown is the weighted mean of the results obtained with the six observables. The weights were given by the reciprocal of the square of the total error on the ratios $\alpha_s^c/\alpha_s^{\text{uds}}$ and $\alpha_s^b/\alpha_s^{\text{uds}}$ given in Tables 10 and 11. The statistical error on the mean was calculated taking into account correlations between the five observables. The correlation matrix was calculated from 100 Monte Carlo event samples. The systematic uncertainty on the weighted mean was determined from the change in the mean that occurred when each systematic check was applied to all the event shape distributions simultaneously. The mean values of $\alpha_s^c/\alpha_s^{\text{uds}}$ and $\alpha_s^b/\alpha_s^{\text{uds}}$ were determined to be

$$\begin{aligned} \alpha_s^c/\alpha_s^{\text{uds}} &= 0.997 \pm 0.038 \text{ (stat.)} \pm 0.030 \text{ (syst.)} \\ &\quad \pm 0.012 \text{ (theory)} \\ \alpha_s^b/\alpha_s^{\text{uds}} &= 0.993 \pm 0.008 \text{ (stat.)} \pm 0.006 \text{ (syst.)} \\ &\quad \pm 0.011 \text{ (theory)} . \end{aligned}$$

In both cases the results are consistent with unity, indicating flavour independence of α_s .

As shown in Table 11, the largest experimental systematic error on the results obtained from the variable y_{23} originated from moving the lower bound of the fit range from $y_{23} = 0.015$ to 0.025. It was found that this relatively large variation in the result was due to a small discrepancy between the data and the Monte Carlo, of the order of a few percent, for values of $y_{23} < 0.03$. If one excludes

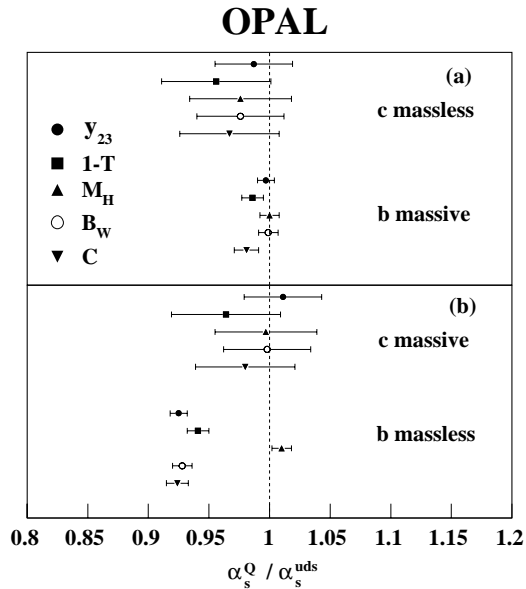


Fig. 8a,b. The ratios $\alpha_s^c/\alpha_s^{uds}$ and $\alpha_s^b/\alpha_s^{uds}$ determined in two different ways: **a** where the uds and c quarks were treated as if massless and the b quark was considered to be massive and **b** where the uds and b quark were treated as massless and the c quark was considered massive. The errors shown are statistical only

the results obtained from y_{23} from the calculation of the weighted means, the mean value obtained for $\alpha_s^b/\alpha_s^{uds}$ remains unchanged within the experimental precision, while the mean value of $\alpha_s^c/\alpha_s^{uds}$ changes from 0.997 to 0.990.

The size of the mass effect for c and b quarks and its relevance to the measurement of α_s are also of interest. From phase space considerations one can estimate the size of the mass effects for 3-jet observables. The ratio of the phase space of two massive quarks and a gluon to the phase space for three massless particles is $1 + 8(M_q/M_Z)^2 \log(M_q/M_Z)$ [37]. This represents a 7% effect for $M_q = 5 \text{ GeV}/c^2$ and 0.7% for $M_q = 1.35 \text{ GeV}/c^2$.

Figure 8a shows the ratios $\alpha_s^c/\alpha_s^{uds}$ and $\alpha_s^b/\alpha_s^{uds}$ determined using $\mathcal{O}(\alpha_s^2)$ massless calculations for both uds and c quarks and $\mathcal{O}(\alpha_s^2)$ massive calculations for b quarks. Again we show the average of fits with $x_\mu = 1.0$ and x_μ as a free parameter. One sees a small systematic shift of $\alpha_s^c/\alpha_s^{uds}$ with respect to the fits with the massive calculation. Due to the large statistical error on the measurements with c quark events it is not possible to determine the exact size of the mass effect which, from arguments presented above, is expected to be of order 1%. In Fig. 8b, $\alpha_s^c/\alpha_s^{uds}$ and $\alpha_s^b/\alpha_s^{uds}$ were determined using massless calculations for uds and b quarks and massive calculations for c quarks. In this case $\alpha_s^b/\alpha_s^{uds}$ shows a large systematic shift of order 5 to 7%. It should be noted that the values of α_s^{uds} and $\alpha_s^c/\alpha_s^{uds}$ remained unchanged within their statistical errors with respect to the results presented in Fig. 7, therefore the change in $\alpha_s^b/\alpha_s^{uds}$ can be attributed entirely to changes in α_s^b . This sensitivity to the b quark pole mass (M_b) suggests that this effect could be exploited, as in [12], to measure M_b itself, by assuming flavour independence

of α_s and fitting for M_b . Preliminary investigations show an apparent correlation between the value of M_b in JETSET, which is used for hadronization corrections, and the measured value of M_b , making a determination of the systematic error due to the choice of M_b in JETSET difficult. This point is still under investigation in hopes of making a future determination of M_b using this technique.

As expected, fits to M_H do not exhibit the mass effect like the other variables do. Here the quark mass fixes a lower bound of the M_H distribution since the invariant mass of the jet cannot be less than the mass of the quark that originates the jet. For $M_b = 5.0 \text{ GeV}$ the lower bound lies at about $M_H/\sqrt{s} = 0.05$, which is well outside of the fit range.

10 Conclusion

We have presented a test of the flavour independence of the strong coupling constant for charm and bottom quarks with respect to light (uds) quarks. This analysis was based on a sample of hadronic decays of the Z^0 resonance recorded by the OPAL detector at LEP. The global event shapes y_{23} , $1 - T$, M_H , B_W and C were used to measure α_s in three flavour tagged event samples (uds, c and b). The event shape distributions were fitted by $\mathcal{O}(\alpha_s^2)$ calculations of jet production taking into account mass effects for the c and b quarks. The ratios $\alpha_s^c/\alpha_s^{uds}$ and $\alpha_s^b/\alpha_s^{uds}$ were both found to be consistent with unity, indicating the flavour independence of α_s . These results are in agreement with those of DELPHI [12] and SLD [13] who performed tests of flavour independence of α_s where heavy quark mass effects were taken into account.

The measurement of $\alpha_s^c/\alpha_s^{uds}$ achieved a precision of 5%. The relatively large statistical error was due to the low efficiency for tagging c quark events ($\approx 2\%$) which relied on finding D^{*+} mesons. The experimental error was dominated by varying the cut on the scaled energy of the D^{*+} mesons which was required to reduce the background from c quark events coming from cascade decays of b hadrons. The measurement of $\alpha_s^b/\alpha_s^{uds}$ achieved a 1.5% precision, the error being dominated by the theoretical systematic error. The largest theoretical errors were due to uncertainties in the b quark mass and the renormalization scale factor x_μ .

In addition, we have presented a study of the effect of heavy quark masses on global event shape variables. It was observed that the values of α_s determined from y_{23} , $1 - T$, B_W and C were reduced by 5 to 7% when these event shapes were measured with a sample of b quark events and a massless QCD calculation was used. The shape variable M_H was found to be insensitive to the b quark mass.

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References

- H. Fritzsch, M. Gell-Mann, 16th Int. Conf. on High Energy Physics, Chicago (1972); H. Fritzsch, M. Gell-Mann and H. Leutwyler, Phys. Lett. **B 47** (1973) 365; D. Gross and F. Wilczek, Phys. Rev. Lett. **30** (1973) 1343; H.D. Politzer, Phys. Rev. Lett. **30** (1973) 1346.
- OPAL Collaboration: R. Akers et al., Z. Phys. **C 60** (1993) 397.
- OPAL Collaboration: R. Akers et al., Z. Phys. **C 65** (1995) 31.
- L3 Collaboration: B. Adeva et al., Phys. Lett. **B 271** (1991) 461.
- DELPHI Collaboration: P. Abreu et al., Phys. Lett. **B 307** (1993) 221.
- ALEPH Collaboration: D. Buskulic et al., Phys. Lett. **B 355** (1995) 381.
- SLD Collaboration: K. Abe et al., Phys. Rev. **D 53** (1996) 2271.
- A. Ballestrero, E. Maina and S. Moretti, Phys. Lett. **B 294** (1992) 425; A. Ballestrero, E. Maina and S. Moretti, Nucl. Phys. **B 415** (1994) 265.
- G. Rodrigo, Nucl. Phys. Proc. Suppl. **A54** (1997) 60; G. Rodrigo, A. Santamaria and M. Bilenkii, Phys. Rev. Lett. **79** (1997) 193.
- W. Bernreuther, A. Brandenburg and P. Uwer, Phys. Rev. Lett. **79** (1997) 189.
- P. Nason and C. Oleari, Nucl. Phys. **B521** (1998) 237.
- DELPHI Collaboration: P. Abreu et al., Phys. Lett. **B 418** (1998) 430.
- SLD Collaboration: K. Abe et al., Phys. Rev. **D 59** (1999) 12002.
- OPAL Collaboration: K. Ahmet et al., Nucl. Instr. and Meth. **A 305** (1991) 275; P.P. Allport et al., Nucl. Instr. and Meth. **A 324** (1993) 34.
- P.P. Allport et al., Nucl. Instr. and Meth. **A 346** (1994) 476.
- OPAL Collaboration: G. Alexander et al., Z. Phys. **C 52** (1991) 175.
- OPAL Collaboration: P. D. Acton et al., Z. Phys. **C 59** (1993) 1.
- T. Sjöstrand, Comp. Phys. Comm. **82** (1994) 74.
- OPAL Collaboration: G. Alexander et al., Z. Phys. **C 69** (1996) 543.
- C. Peterson et al., Phys. Rev. **D 27** (1983) 105.
- J. Allison et al., Nucl. Instr. and Meth. **A 317** (1991) 47.
- OPAL Collaboration, P. D. Acton et al., Z. Phys. **C 58** (1993) 523.
- OPAL Collaboration, G. Abbiendi et al., *A Measurement of R_b using a Double Tagging Method*, **CERN-EP/98-137** (1998). To be published in *Eur. Phys. J. C*
- OPAL Collaboration: R. Akers et al., Z. Phys. **C 67** (1995) 27; OPAL Collaboration: R. Akers et al., Phys. Lett. **B 353** (1995) 595.
- M.H. Seymour, Nucl. Phys. **B 436** (1995) 163.
- Particle Data Group: C. Caso et al., Eur. Phys. J. **C 3**, (1998).
- OPAL Collaboration: K. Ackerstaff et al., Eur. Phys. J. **C 1** (1998) 439.
- OPAL Collaboration: P. D. Acton et al., Z. Phys. **C 55** (1992) 1.
- B. Andersson, G. Gustafson, G. Ingelman and T. Sjöstrand, Phys. Rep. **97** (1983) 31.
- R.K. Ellis, D.A. Ross and A.E. Terrano, Nucl. Phys. **B 178** (1981) 421.
- C. Oleari, PhD Thesis, Università degli Studi di Milano, **IFUM-607-FT** (1997), and **hep-ph/9802431**.
- QCD, Z. Kunszt and P. Nason [conv.], *Z Physics at LEP 1*, G. Altarelli, R. Kleiss and C. Verzegnassi, editors, volume 1, **CERN 89-08**.
- ALEPH Collaboration: D. Decamp et al., Phys. Lett. **B 284** (1992) 408; DELPHI Collaboration: P. Abreu et al., Z. Phys. **C 59** (1993) 21; L3 Collaboration: M. Acciarri et al., Phys. Lett. **B 404** (1997) 390; SLD Collaboration: K. Abe et al., Phys. Rev. **D 51** (1995) 962.
- DELPHI Collaboration: P. Areu et al. Z. Phys. **C 54** (1992) 55.
- L. Lönnbald, Comp. Phys. Comm. **71** (1992) 15.
- G. Marchesini, B.R. Webber, Nucl. Phys. **B310** (1988) 461; G. Marchesini et. al., Comput. Phys. Commun. **67** (1992) 465.
- G. Rodrigo, PhD Thesis, Universitat de València, 1996, **hep-ph/9703359** and ISBN:84-370-2989-9.